

Package ‘hdi’

July 22, 2025

Type Package

Title High-Dimensional Inference

Version 0.1-10

Date 2025-05-15

Author Lukas Meier [aut, cre],
Ruben Dezeure [aut],
Nicolai Meinshausen [aut],
Martin Maechler [aut],
Peter Buehlmann [aut]

Maintainer Lukas Meier <meier@stat.math.ethz.ch>

Description Implementation of multiple approaches to perform inference in high-dimensional models.

Depends scalreg

DependsNote scalreg does not correctly import lars etc, so we need to depend on it

Imports grDevices, graphics, stats, parallel, MASS, glmnet, linprog

Suggests Matrix

SuggestsNote for tests only

Encoding UTF-8

License GPL

NeedsCompilation no

Repository CRAN

Date/Publication 2025-04-17 14:50:02 UTC

Contents

hdi-package	2
boot.lasso.proj	4
clusterGroupBound	6
fdr.adjust	9
glm.pval	10

groupBound	11
hdi	13
lasso.cv	15
lasso.firstq	16
lasso.proj	17
lm.ci	19
lm.pval	20
multi.split	21
plot.clusterGroupBound	24
riboflavin	25
ridge.proj	26
rXb	28
stability	30
Index	32

hdi-package

hdi

Description

Implementation of multiple approaches to perform inference in high-dimensional models.

Details

The DESCRIPTION file:

```

Package:      hdi
Type:         Package
Title:        High-Dimensional Inference
Version:      0.1-10
Date:         2025-05-15
Authors@R:   c(person(given = "Lukas", family = "Meier", role = c("aut", "cre"), email = "meier@stat.math.ethz.ch"), pers
Author:       Lukas Meier [aut, cre], Ruben Dezeure [aut], Nicolai Meinshausen [aut], Martin Maechler [aut], Peter Buehl
Maintainer:   Lukas Meier <meier@stat.math.ethz.ch>
Description:  Implementation of multiple approaches to perform inference in high-dimensional models.
Depends:      scalreg
DependsNote:  scalreg does not correctly import lars etc, so we need to depend on it
Imports:      grDevices, graphics, stats, parallel, MASS, glmnet, linprog
Suggests:     Matrix
SuggestsNote: for tests only
Encoding:     UTF-8
License:      GPL

```

Index of help topics:

boot.lasso.proj	P-values based on the bootstrapped lasso projection method
clusterGroupBound	Hierarchical structure group tests in linear model
fdr.adjust	Function to calculate FDR adjusted p-values
glm.pval	Function to calculate p-values for a generalized linear model.
groupBound	Lower bound on the l1-norm of groups of regression variables
hdi	Function to perform inference in high-dimensional (generalized) linear models
hdi-package	hdi
lasso.cv	Select Predictors via (10-fold) Cross-Validation of the Lasso
lasso.firstq	Determine the first q Predictors in the Lasso Path
lasso.proj	P-values based on lasso projection method
lm.ci	Function to calculate confidence intervals for ordinary multiple linear regression.
lm.pval	Function to calculate p-values for ordinary multiple linear regression.
multi.split	Calculate P-values Based on Multi-Splitting Approach
plot.clusterGroupBound	Plot output of hierarchical testing of groups of variables
rXb	Generate Data Design Matrix X and Coefficient Vector beta
riboflavin	Riboflavin data set
ridge.proj	P-values based on ridge projection method
stability	Function to perform stability selection

Author(s)

Lukas Meier, Ruben Dezeure, Nicolai Meinshausen, Martin Mächler, Peter Bühlmann, Maintainer: Lukas Meier <meier@stat.math.ethz.ch>

References

- Dezeure, R., Bühlmann, P., Meier, L. and Meinshausen, N. (2015) High-dimensional inference: confidence intervals, p-values and R-software hdi. *Statistical Science* **30**, 533–558.
- Meinshausen, N., Meier, L. and Bühlmann, P. (2009) P-values for high-dimensional regression. *Journal of the American Statistical Association* **104**, 1671–1681.
- Meinshausen, N. (2015) Group-bound: confidence intervals for groups of variables in sparse high-dimensional regression without assumptions on the design. *Journal of the Royal Statistical Society: Series B*, **77**(5), 923–945.
- Meinshausen, N. and Bühlmann, P. (2010) Stability selection (with discussion). *Journal of the Royal Statistical Society: Series B* **72**, 417–473.

boot.lasso.proj *P-values based on the bootstrapped lasso projection method*

Description

Compute p-values based on the lasso projection method, also known as the de-sparsified Lasso, using the bootstrap to approximate the distribution of the estimator.

Usage

```
boot.lasso.proj(x, y, family = "gaussian", standardize = TRUE,
               multiplecorr.method = "WY",
               parallel = FALSE, ncores = getOption("mc.cores", 2L),
               betainit = "cv lasso", sigma = NULL, Z = NULL, verbose = FALSE,
               return.Z = FALSE, robust = FALSE,
               B = 1000, boot.shortcut = FALSE,
               return.bootdist = FALSE, wild = FALSE,
               gaussian.stub = FALSE)
```

Arguments

x	Design matrix (without intercept).
y	Response vector.
family	family
standardize	Should design matrix be standardized to unit column standard deviation.
multiplecorr.method	Either "WY" or any of p.adjust.methods .
parallel	Should parallelization be used? (logical)
ncores	Number of cores used for parallelization.
betainit	Either a numeric vector, corresponding to a sparse estimate of the coefficient vector, or the method to be used for the initial estimation, "scaled lasso" or "cv lasso".
sigma	Estimate of the standard deviation of the error term. This estimate needs to be compatible with the initial estimate (see betainit) provided or calculated. Otherwise, results will not be correct.
Z	user input, also see return.Z below
verbose	A boolean to enable reporting on the progress of the computations. (Only prints out information when Z is not provided by the user)
return.Z	An option to return the intermediate result which only depends on the design matrix x. This intermediate results can be used when calling the function again and the design matrix is the same as before.
robust	Uses a robust variance estimation procedure to be able to deal with model misspecification.

B	The number of bootstrap samples to be used.
boot.shortcut	A boolean to enable the computational shortcut for the bootstrap. If set to true, the lasso is not re-tuned for each bootstrap iteration, but it uses the tuning parameter computed on the original data instead.
return.bootdist	A boolean specifying if one is to return the computed bootstrap distributions to the estimator. (Matrix size: $\text{ncol}(x)*B$) If the multiple testing method was chosen to be WY, the bootstrap distribution computer under the complete null hypothesis is returned as well. This option is required if one wants to compute confidence intervals afterwards.
wild	Perform the wild bootstrap based on $N(0,1)$ distributed random variables
gaussian.stub	DEVELOPER OPTION. Only enable if you know what you are doing. A boolean to run stub code instead of actually bootstrapping the estimator. It generates a finite sample distribution for each estimate by sampling B samples from $N(0, \hat{\text{s.e.}}_j^2)$. (Note: we do not sample from the multivariate gaussian with the covariance matrix. Therefore, no dependencies are modelled at all.) Useful for debugging and for checking if the bootstrap is way off for some reason.

Value

pval	Individual p-values for each parameter.
pval.corr	Multiple testing corrected p-values for each parameter.
sigmahat	$\hat{\sigma}$ coming from the scaled lasso.
Z	Only different from NULL if the option return.Z is on. This is an intermediate result from the computation which only depends on the design matrix x. These are the residuals of the nodewise regressions.
B	The number of bootstrap samples used.
boot.shortcut	If the bootstrap shortcut has been used or not.
lambda	What tuning parameter was used for the bootstrap shortcut. NULL if no shortcut was used or if no valid lambda was available to use for the shortcut.
cboot.dist	Only different from NULL if the option return.bootdist is on. This is a $\text{ncol}(x)*B$ matrix where each row contains the computed centered bootstrap distribution for that estimate.
cboot.dist.underH0	Only different from NULL if the option return.bootdist is on and if the multiple testing method is WY. This is a $\text{ncol}(x)*B$ matrix where each row contains the computed centered bootstrap distribution for that estimate. These bootstrap distributions were computed under the complete null hypothesis ($b_1 = \dots = b_p = 0$).

Author(s)

Ruben Dezeure

References

- van de Geer, S., Bühlmann, P., Ritov, Y. and Dezeure, R. (2014) On asymptotically optimal confidence regions and tests for high-dimensional models. *Annals of Statistics* **42**, 1166–1202.
- Zhang, C., Zhang, S. (2014) Confidence intervals for low dimensional parameters in high dimensional linear models. *Journal of the Royal Statistical Society: Series B* **76**, 217–242.
- Bühlmann, P. and van de Geer, S. (2015) High-dimensional inference in misspecified linear models. *Electronic Journal of Statistics* **9**, 1449–1473.
- Dezeure, R., Bühlmann, P. and Zhang, C. (2016) High-dimensional simultaneous inference with the bootstrap <http://arxiv.org/abs/1606.03940>

Examples

```
x <- matrix(rnorm(100 * 10), nrow = 100, ncol = 10)
y <- x[,1] + x[,2] + rnorm(100)

fit.lasso <- boot.lasso.proj(x, y)
which(fit.lasso$pval.corr < 0.05) # typically: '1' and '2' and no other

## Use the computational shortcut for the bootstrap to speed up
## computations
fit.lasso.shortcut <- boot.lasso.proj(x, y, boot.shortcut = TRUE)
which(fit.lasso.shortcut$pval.corr < 0.05) # typically: '1' and '2' and no other

## Return the bootstrap distribution as well and compute confidence intervals based on it
fit.lasso.allinfo <- boot.lasso.proj(x, y, return.bootdist = TRUE)
confint(fit.lasso.allinfo, level = 0.95)
confint(fit.lasso.allinfo, parm = 1:3)

## Use the scaled lasso for the initial estimate
fit.lasso.scaled <- boot.lasso.proj(x, y, betainit = "scaled lasso")
which(fit.lasso.scaled$pval.corr < 0.05)

## Use a robust estimate for the standard error
fit.lasso.robust <- boot.lasso.proj(x, y, robust = TRUE)
which(fit.lasso.robust$pval.corr < 0.05)
```

clusterGroupBound

Hierarchical structure group tests in linear model

Description

Computes confidence intervals for the ℓ_1 -norm of groups of linear regression coefficients in a hierarchical clustering tree.

Usage

```
clusterGroupBound(x, y, method = "average",
                  dist = as.dist(1 - abs(cor(x))), alpha = 0.05,
                  eps = 0.1, hcloutput, nsplit = 11,
                  s = min(10, ncol(x) - 1),
                  silent = FALSE, setseed = TRUE, lpSolve = TRUE)
```

Arguments

x	numeric design matrix of the regression $n \times p$ with p columns for p predictor variables and n rows corresponding to n observations.
y	numeric response variable of length n .
method	a character string; the method used for constructing the hierarchical clustering tree (default: "average" for "average linkage") via hclust . Alternatively, you can provide your own hierarchical clustering through the optional argument hcloutput .
dist	a distance matrix can be specified on which the hierarchical clustering will be based (see dist). The default option is that the distance between variables will be calculated as 1 less the absolute correlation matrix. Alternatively, you can provide your own hierarchical clustering through the optional argument hcloutput .
alpha	numeric level in (0, 1) at which the test / confidence intervals are to be constructed.
eps	a level of $\text{eps} \times \text{alpha}$ is used and the values of different splits are aggregated using the (1-eps) quantile. See reference below for more details.
hcloutput	optionally, the value of a hclust () call. If it is provided, the arguments dist and method are ignored.
nsplit	the number of data splits used.
s	the dimensionality of the projection that is used. Lower values lead to faster computation and if $n > 50$, then s is set to 50 if left unspecified, to avoid lengthy computations.
silent	logical enabling progress output.
setseed	a logical; if this is true (recommended), then the same random seeds are used for all groups, which makes the confidence intervals simultaneously valid over all groups of variables tested.
lpSolve	logical; only set it to false if lpSolve () is not working on the current machine: setting it to false will result in much slower computations; only use on small problems.

Value

Returns a list with components

groupNumber	The index of the group tested in the original hierarchical clustering tree
members	A list containing the variables that belong into each testes group

noMembers	A vector containing the number of members in each group
lowerBound	The lower bound on the l1-norm in each group
position	The position on the x-axis of each group (used for plotting)
leftChild	Gives the index of the group that corresponds to the left child node in the tested tree (negative values correspond to leaf nodes)
rightChild	Same as leftChild for the right child of each node
isLeaf	Logical vector. Is TRUE for a group if it is a leaf node in the tested tree or if both child nodes have a zero lower bound on their group l1-norm

Author(s)

Nicolai Meinshausen

References

Meinshausen, N. (2015); JRSS B, see [groupBound](#).

See Also

Use [groupBound](#) to compute the lower bound for selected groups of variables whereas you use this `clusterGroupBound` to test all groups in a hierarchical clustering tree.

Examples

```
## Create a regression problem with correlated design (n = 10, p = 3):
## a block of size 2 and a block of size 1, within-block correlation is 0.99

set.seed(29)
p <- 3
n <- 10

Sigma <- diag(p)
Sigma[1,2] <- Sigma[2,1] <- 0.99

x <- matrix(rnorm(n * p), nrow = n) %%% chol(Sigma)

## Create response with active variable 1
beta <- rep(0, p)
beta[1] <- 5

y <- as.numeric(x %%% beta + rnorm(n))

out <- clusterGroupBound(x, y, nsplit = 4) ## use larger value for nsplit!

## Plot and print the hierarchical group-test
plot(out)
print(out)
out$members
out$lowerBound
```

fdr.adjust	<i>Function to calculate FDR adjusted p-values</i>
------------	--

Description

Calculates FDR adjusted p-values similar to R-function p.adjust but **without** adjustment for multiplicity.

Usage

```
fdr.adjust(p)
```

Arguments

p Vector of p-values.

Details

It is assumed that the p-values are already corrected for multiplicity. P-values with a value of 1 are currently ignored.

Value

Vector of p-values.

Author(s)

Lukas Meier

References

Meinshausen, N., Meier, L. and Bühlmann, P. (2009), *P-values for high-dimensional regression*, Journal of the American Statistical Association 104, 1671-1681.

See Also

[p.adjust](#)

Examples

```
x <- matrix(rnorm(100 * 1000), nrow = 100, ncol = 1000)
y <- x[,1] * 2 + x[,2] * 2.5 + rnorm(100)

## Multi-splitting with lasso.firstq as model selector function
fit.multi <- multi.split(x, y, model.selector = lasso.firstq,
                        args.model.selector = list(q = 10))
p.adjust <- fdr.adjust(fit.multi$pval.corr)
```

`glm.pval`*Function to calculate p-values for a generalized linear model.*

Description

Calculates (classical) p-values for an ordinary generalized linear model in the $n > p$ situation.

Usage

```
glm.pval(x, y, family = "binomial", verbose = FALSE, ...)
```

Arguments

<code>x</code>	Design matrix (without intercept).
<code>y</code>	Response vector.
<code>family</code>	As in glm .
<code>verbose</code>	Logical. Should information be printed out if algorithm did not converge?
<code>...</code>	Additional arguments to be passed to glm .

Details

A model with intercept is fitted but the p-value of the intercept is not reported in the output.

Value

Vector of p-values (not including the intercept).

Author(s)

Lukas Meier

See Also

[hdi](#)

Examples

```
## ...
```

groupBound

*Lower bound on the l1-norm of groups of regression variables***Description**

Computes a lower bound that forms a one-sided confidence interval for the group l1-norm of a specified group of regression parameters. It is assumed that errors have a Gaussian distribution with unknown noise level. The underlying vector that inference is made about is the l1-sparsest approximation to the noiseless data.

Usage

```
groupBound(x, y, group, alpha = 0.05, eps = 0.1, nsplit = 11,
           s = min(10, ncol(x) - 1), setseed = TRUE,
           silent = FALSE, lpSolve = TRUE, parallel = FALSE,
           ncores = getOption("mc.cores", 2L))
```

Arguments

x	numeric design matrix of the regression $n \times p$ with p columns for p predictor variables and n rows corresponding to n observations.
y	numeric response variable of length n .
group	either a numeric vector with entries in $\{1, \dots, p\}$ or a list with such numeric vectors. If group is a numeric vector, this is the group of variables for which a lower bound is computed. If group is a list, the lower bound is computed for each group in the list.
alpha	numeric level in $(0, 1)$ at which the test / confidence interval is computed.
eps	a level of $\text{eps} * \text{alpha}$ is used and the values of different splits are aggregated using the $(1 - \text{eps})$ quantile. See reference below for more details.
nsplit	the number of data splits used.
s	the dimensionality of the projection that is used. Lower values lead to faster computation and if $n > 50$, then s is set to 50 if left unspecified, to avoid lengthy computations.
setseed	a logical; if this is true (recommended), then the same random seeds are used for all groups, which makes the confidence intervals simultaneously valid over all groups of variables tested.
silent	logical enabling progress output.
lpSolve	logical; only set it to false if lpSolve() is not working on the current machine: setting it to false will result in much slower computations; only use on small problems.
parallel	should parallelization be used? (logical)
ncores	number of cores used for parallelization.

Details

The data are split since the noise level is unknown. On the first part of the random split, a cross-validated lasso solution is computed, using the **glmnet** implementation. This estimator is used as an initial estimator on the second half of the data. Results at level α are aggregated over `nsplit` splits via the median of results at levels $\alpha/2$.

Value

If `group` is a single numeric vector, a scalar containing the lower bound for this group of variables is returned. If `group` is a list, a numeric vector is returned where each entry corresponds to the group of variables defined in the same order in `group`.

Author(s)

Nicolai Meinshausen

References

Meinshausen, N. (2015) Group bound: confidence intervals for groups of variables in sparse high dimensional regression without assumptions on the design. *Journal of the Royal Statistical Society: Series B*, **77**, 923–945; doi:[10.1111/rssb.12094](https://doi.org/10.1111/rssb.12094).

See Also

Use [clusterGroupBound](#) to test all groups in a hierarchical clustering tree.

Examples

```
## Create a regression problem with correlated design: p = 6, n = 50,
## block size B = 3 and within-block correlation of rho = 0.99
p <- 6
n <- 50
B <- 3
rho <- 0.99

ind <- rep(1:ceiling(p / B), each = B)[1:p]
Sigma <- diag(p)

for (ii in unique(ind)){
  id <- which(ind == ii)
  Sigma[id, id] <- rho
}
diag(Sigma) <- 1

x <- matrix(rnorm(n * p), nrow = n) %%% chol(Sigma)

## Create response with active variable 1
beta <- rep(0, p)
beta[1] <- 5

y <- as.numeric(x %%% beta + rnorm(n))
```

```

## Compute lower bounds:

## Lower bound for the L1-norm of *all* variables 1-6 of the sparsest
## optimal vector
nsplit <- 4 ## to make example run fast (use larger value)
lowerBoundAll <- groupBound(x, y, 1:p, nsplit = nsplit)
cat("\nlower bound for all variables 1-6: ", lowerBoundAll, "\n")

## Compute additional lower bounds:
q()## Lower bounds for variable 1 itself, then group {1,3}, 1-2, 1-3, 2-6,
lowerBound <- groupBound(x, y, list(1, c(1,3), 1:2, 1:3, 2:6),
                          nsplit = nsplit)
cat("lower bound for the groups\n\t {1}, {1,3}, {1,2}, {1..3}, {2..6}:\n\t",
    format(formatC(c(lowerBound))), "\n")

```

hdi	<i>Function to perform inference in high-dimensional (generalized) linear models</i>
-----	--

Description

Perform inference in high-dimensional (generalized) linear models using various approaches.

Usage

```

hdi(x, y, method = "multi.split", B = NULL, fraction = 0.5,
    model.selector = NULL, EV = NULL, threshold = 0.75,
    gamma = seq(0.05, 0.99, by = 0.01),
    classical.fit = NULL,
    args.model.selector = NULL, args.classical.fit = NULL,
    verbose = FALSE, ...)

```

Arguments

x	Design matrix (without intercept).
y	Response vector.
method	Multi-splitting ("multi.split") or stability-selection ("stability").
B	Number of sample-splits (for "multi.split") or sub-sample iterations (for "stability"). Default is 50 ("multi.split") or 100 ("stability"). Ignored otherwise.
fraction	Fraction of data used at each of the B iterations.
model.selector	Function to perform model selection. Default is lasso.cv ("multi.split") and lasso.firstq ("stability"). Function must have at least two arguments: x (the design matrix) and y (the response vector). Return value is the index vector of selected columns. See lasso.cv and lasso.firstq for examples. Additional arguments can be passed through <code>args.model.selector</code> .

EV	(only for "stability"). Bound(s) for expected number of false positives . Can be a vector.
threshold	(only for "stability"). Bound on selection frequency.
gamma	(only for "multi.split"). Vector of gamma-values.
classical.fit	(only for "multi.split"). Function to calculate (classical) p-values. Default is lm.pval . Function must have at least two arguments: x (the design matrix) and y (the response vector). Return value is the vector of p-values. See lm.pval for an example. Additional arguments can be passed through <code>args.classical.fit</code> .
args.model.selector	Named list of further arguments for function <code>model.selector</code> .
args.classical.fit	Named list of further arguments for function <code>classical.fit</code> .
verbose	Should information be printed out while computing (logical).
...	Other arguments to be passed to the underlying functions.

Value

pval	(only for "multi.split"). Vector of p-values.
gamma.min	(only for "multi.split"). Value of gamma where minimal p-values was attained.
select	(only for "stability"). List with selected predictors for the supplied values of EV.
EV	(only for "stability"). Vector of corresponding values of EV.
thresholds	(only for "stability"). Used thresholds.
freq	(only for "stability"). Vector of selection frequencies.

Author(s)

Lukas Meier

References

Meinshausen, N., Meier, L. and Bühlmann, P. (2009) P-values for high-dimensional regression. *Journal of the American Statistical Association* **104**, 1671–1681.

Meinshausen, N. and Bühlmann, P. (2010) Stability selection (with discussion). *Journal of the Royal Statistical Society: Series B* **72**, 417–473.

See Also

[stability](#), [multi.split](#)

Examples

```
x <- matrix(rnorm(100 * 200), nrow = 100, ncol = 200)
y <- x[,1] * 2 + x[,2] * 2.5 + rnorm(100)

## Multi-splitting with lasso.firstq as model selector function
fit.multi <- hdi(x, y, method = "multi.split",
```

```

                                model.selector =lasso.firstq,
                                args.model.selector = list(q = 10))
fit.multi
fit.multi$pval.corr[1:10] ## the first 10 p-values

## Stability selection
fit.stab <- hdi(x, y, method = "stability", EV = 2)
fit.stab
fit.stab$freq[1:10] ## frequency of the first 10 predictors

```

lasso.cv

*Select Predictors via (10-fold) Cross-Validation of the Lasso***Description**

Performs (n-fold) cross-validation of the lasso (via [cv.glmnet](#)) and determines the prediction optimal set of parameters.

Usage

```

lasso.cv(x, y,
         nfolds = 10,
         grouped = nrow(x) > 3*nfolds,
         ...)

```

Arguments

x	numeric design matrix (without intercept) of dimension $n \times p$.
y	response vector of length n .
nfolds	the number of folds to be used in the cross-validation
grouped	corresponds to the grouped argument to cv.glmnet . This has a smart default such that glmnet does not give a warning about too small sample size.
...	further arguments to be passed to cv.glmnet .

Details

The function basically only calls [cv.glmnet](#), see source code.

Value

Vector of selected predictors.

Author(s)

Lukas Meier

See Also

[hdi](#) which uses `lasso.cv()` by default; [cv.glmnet](#). An alternative for `hdi()`: [lasso.firstq](#).

Examples

```
x <- matrix(rnorm(100 * 1000), nrow = 100, ncol = 1000)
y <- x[,1] * 2 + x[,2] * 2.5 + rnorm(100)
sel <- lasso.cv(x, y)
sel
```

`lasso.firstq`*Determine the first q Predictors in the Lasso Path*

Description

Determines the q predictors that enter the lasso path first.

Usage

```
lasso.firstq(x, y, q, ...)
```

Arguments

<code>x</code>	numeric design matrix (without intercept) of dimension $n \times p$.
<code>y</code>	response vector of length n .
<code>q</code>	number of predictors that should be selected, a positive integer.
<code>...</code>	optional additional arguments to be passed to glmnet .

Details

The `lasso.firstq` function calls [glmnet](#) in a special way and simply postprocesses its nonzero predictor list, see its source code.

Value

Vector of selected predictors.

Author(s)

Lukas Meier

See Also

[hdi](#); the default choice for `hdi()`, [lasso.cv.glmnet](#)

Examples

```
x <- matrix(rnorm(100 * 1000), nrow = 100, ncol = 1000)
y <- x[,1] * 2 + x[,2] * 2.5 + rnorm(100)
sel <- lasso.firstq(x, y, q = 5)
sel # 5 integers from {1,2, ..., 1000}, including '1' and '2', typically
```

lasso.proj

*P-values based on lasso projection method***Description**

Compute p-values based on the lasso projection method, also known as the de-sparsified Lasso, using an asymptotic gaussian approximation to the distribution of the estimator.

Usage

```
lasso.proj(x, y, family = "gaussian", standardize = TRUE,
           multiplecorr.method = "holm", N = 10000,
           parallel = FALSE, ncores = getOption("mc.cores", 2L),
           betainit = "cv lasso", sigma = NULL, Z = NULL, verbose = FALSE,
           return.Z = FALSE, suppress.grouptesting = FALSE, robust = FALSE,
           do.ZnZ = FALSE)
```

Arguments

x	Design matrix (without intercept).
y	Response vector.
family	family
standardize	Should design matrix be standardized to unit column standard deviation.
multiplecorr.method	Either "WY" or any of p.adjust.methods .
N	Number of empirical samples (only used if multiplecorr.method == "WY")
parallel	Should parallelization be used? (logical)
ncores	Number of cores used for parallelization.
betainit	Either a numeric vector, corresponding to a sparse estimate of the coefficient vector, or the method to be used for the initial estimation, "scaled lasso" or "cv lasso".
sigma	Estimate of the standard deviation of the error term. This estimate needs to be compatible with the initial estimate (see betainit) provided or calculated. Otherwise, results will not be correct.
Z	user input, also see return.Z below
verbose	A boolean to enable reporting on the progress of the computations. (Only prints out information when Z is not provided by the user)

<code>return.Z</code>	An option to return the intermediate result which only depends on the design matrix x . This intermediate results can be used when calling the function again and the design matrix is the same as before.
<code>suppress.grouptest</code>	A boolean to optionally suppress the preparations made for testing groups. This will avoid quite a bit of computation and memory usage. The output will also be smaller.
<code>robust</code>	Uses a robust variance estimation procedure to be able to deal with model misspecification.
<code>do.ZnZ</code>	Use a slightly different way of choosing tuning parameters to compute Z , called $Z\&Z$ based on Zhang and Zhang (2014). This choice of tuning parameter results in a slightly higher variance of the estimator. More concretely, it achieves a 25 variance of the estimator (over $j=1..ncol(x)$) in comparison to tuning with cross-validation.

Value

<code>pval</code>	Individual p-values for each parameter.
<code>pval.corr</code>	Multiple testing corrected p-values for each parameter.
<code>groupTest</code>	Function to perform groupwise tests. Groups are indicated using an index vector with entries in $\{1, \dots, p\}$ or a list thereof.
<code>clusterGroupTest</code>	Function to perform groupwise tests based on hierarchical clustering. You can either provide a distance matrix and clustering method or the output of hierarchical clustering from the function <code>hclust</code> as for <code>clusterGroupBound</code> . P-values are adjusted for multiple testing.
<code>sigmahat</code>	$\hat{\sigma}$ coming from the scaled lasso.
<code>Z</code>	Only different from NULL if the option <code>return.Z</code> is on. This is an intermediate result from the computation which only depends on the design matrix x . These are the residuals of the nodewise regressions.

Author(s)

Ruben Dezeure

References

- van de Geer, S., Bühlmann, P., Ritov, Y. and Dezeure, R. (2014) On asymptotically optimal confidence regions and tests for high-dimensional models. *Annals of Statistics* **42**, 1166–1202.
- Zhang, C., Zhang, S. (2014) Confidence intervals for low dimensional parameters in high dimensional linear models. *Journal of the Royal Statistical Society: Series B* **76**, 217–242.
- Bühlmann, P. and van de Geer, S. (2015) High-dimensional inference in misspecified linear models. *Electronic Journal of Statistics* **9**, 1449–1473.

Examples

```

x <- matrix(rnorm(100 * 10), nrow = 100, ncol = 10)
y <- x[,1] + x[,2] + rnorm(100)
fit.lasso <- lasso.proj(x, y)
which(fit.lasso$pval.corr < 0.05) # typically: '1' and '2' and no other

## Group-wise testing of the first two coefficients
fit.lasso$groupTest(1:2)

##Compute confidence intervals
confint(fit.lasso, level = 0.95)

## Hierarchical testing using distance matrix based on
## correlation matrix
out.clust <- fit.lasso$clusterGroupTest()
plot(out.clust)

## Fit the lasso projection method without doing the preparations
## for group testing (saves time and memory)
fit.lasso.faster <- lasso.proj(x, y, suppress.grouptesting = TRUE)

## Use the scaled lasso for the initial estimate
fit.lasso.scaled <- lasso.proj(x, y, betainit = "scaled lasso")
which(fit.lasso.scaled$pval.corr < 0.05)

## Use a robust estimate for the standard error
fit.lasso.robust <- lasso.proj(x, y, robust = TRUE)
which(fit.lasso.robust$pval.corr < 0.05)

## Perform the Z&Z version of the lasso projection method
fit.lasso <- lasso.proj(x, y, do.ZnZ = TRUE)

which(fit.lasso$pval.corr < 0.05) # typically: '1' and '2' and no other

```

lm.ci

Function to calculate confidence intervals for ordinary multiple linear regression.

Description

Calculates (classical) confidence intervals for an ordinary multiple linear regression model in the $n > p$ situation.

Usage

```
lm.ci(x, y, level = 0.95, ...)
```

Arguments

x	Design matrix (without intercept).
y	Response vector.
level	Coverage level.
...	Additional arguments to be passed to lm .

Details

A model with intercept is fitted but the p-value of the intercept is not reported in the output.

Value

Matrix of confidence interval bounds (not including the intercept).

Author(s)

Lukas Meier

See Also

[hdi](#)

Examples

```
x <- matrix(rnorm(100 * 5), nrow = 100, ncol = 5)
y <- x[,1] * 2 + x[,2] * 2.5 + rnorm(100)
ci <- lm.ci(x, y)
ci
```

lm.pval

Function to calculate p-values for ordinary multiple linear regression.

Description

Calculates (classical) p-values for an ordinary multiple linear regression in the $n > p$ situation.

Usage

```
lm.pval(x, y, exact = TRUE, ...)
```

Arguments

x	Design matrix (without intercept).
y	Response vector.
exact	Logical. TRUE if p-values based on t-distribution should be calculated. FALSE if normal distribution should be used as approximation.
...	Additional arguments to be passed to lm .

Details

A model with intercept is fitted but the p-value of the intercept is not reported in the output.

Value

Vector of p-values (not including the intercept).

Author(s)

Lukas Meier

See Also

[hdi](#)

Examples

```
x <- matrix(rnorm(100 * 5), nrow = 100, ncol = 5)
y <- x[,1] * 2 + x[,2] * 2.5 + rnorm(100)
pval <- lm.pval(x, y)
pval
```

multi.split

Calculate P-values Based on Multi-Splitting Approach

Description

Calculate p-values and confidence intervals based on the multi-splitting approach

Usage

```
multi.split(x, y, B = 100, fraction = 0.5, ci = TRUE, ci.level = 0.95,
            model.selector = lasso.cv,
            classical.fit = lm.pval, classical.ci = lm.ci,
            parallel = FALSE, ncores = getOption("mc.cores", 2L),
            gamma = seq(ceiling(0.05 * B) / B, 1 - 1 / B, by = 1 / B),
            args.model.selector = NULL, args.classical.fit = NULL,
            args.classical.ci = NULL,
            return.nonaggr = FALSE, return.selmodels = FALSE,
            repeat.max = 20,
            verbose = FALSE)
```

Arguments

<code>x</code>	numeric design matrix (without intercept).
<code>y</code>	numeric response vector.
<code>B</code>	the number of sample-splits, a positive integer.
<code>fraction</code>	a number in $(0, 1)$, the fraction of data used at each sample split for the model selection process. The remaining data is used for calculating the p-values.
<code>ci</code>	logical indicating if a confidence interval should be calculated for each parameter.
<code>ci.level</code>	(if <code>ci</code> is true:) a number in $(0, 1)$, typically close to 1, the desired coverage level of the confidence intervals.
<code>model.selector</code>	a function to perform model selection, with default lasso.cv . The function must have at least two arguments, <code>x</code> (the design matrix) and <code>y</code> (the response vector). Return value is the index vector of selected columns. See lasso.cv and lasso.firstq for an example. Additional arguments can be passed via <code>args.model.selector</code> .
<code>classical.fit</code>	a function to calculate (classical) p-values. Default is lm.pval . The function must have at least two arguments, <code>x</code> (the design matrix) and <code>y</code> (the response vector), and return the vector of p-values. See lm.pval for an example. Additional arguments can be passed through <code>args.classical.fit</code> .
<code>classical.ci</code>	a function to calculate (classical) confidence intervals. Default is lm.ci . The function must have at least 3 arguments, <code>x</code> (the design matrix), <code>y</code> (the response vector) and <code>level</code> (the coverage level), and return the matrix of confidence intervals. See lm.ci for an example. Additional arguments can be passed through <code>args.classical.ci</code> .
<code>parallel</code>	logical indicating if parallelization via mclapply should be used.
<code>ncores</code>	number of cores used for parallelization as <code>mc.cores</code> in mclapply() .
<code>gamma</code>	vector of gamma-values. In case gamma is a scalar, the value Q_j instead of P_j is being calculated (see reference below).
<code>args.model.selector</code>	named list of further arguments for function <code>model.selector</code> .
<code>args.classical.fit</code>	named list of further arguments for function <code>classical.fit</code> .
<code>args.classical.ci</code>	named list of further arguments for function <code>classical.ci</code> .
<code>return.nonaggr</code>	logical indicating if the unadjusted p-values be returned.
<code>return.selmodels</code>	logical indicating if the selected models (at each split) should be returned. Necessary for the <code>clusterGroupTest()</code> part of the result.
<code>repeat.max</code>	positive integer indicating the maximal number of split trials. Should not matter in regular cases, but necessary to prevent infinite loops in borderline cases.
<code>verbose</code>	should information be printed out while computing? (logical).

Value

pval.corr Vector of multiple testing corrected p-values.
 gamma.min Value of gamma where minimal p-values was attained.
 clusterGroupTest
 Function to perform groupwise tests based on hierarchical clustering. You can either provide a distance matrix and clustering method or the output of hierarchical clustering from the function [hclust](#) as for [clusterGroupBound](#). P-values are adjusted for multiple testing.

Author(s)

Lukas Meier, Ruben Dezeure, Jacopo Mandozzi

References

Meinshausen, N., Meier, L. and Bühlmann, P. (2009) P-values for high-dimensional regression. *Journal of the American Statistical Association* **104**, 1671–1681.

Mandozzi, J. and Bühlmann, P. (2015) A sequential rejection testing method for high-dimensional regression with correlated variables. To appear in the *International Journal of Biostatistics*. Preprint arXiv:1502.03300

See Also

[lasso.cv](#), [lasso.firstq](#); [lm.pval](#), [lm.ci](#).

Examples

```
n <- 40 # a bit small, to keep example "fast"
p <- 256
x <- matrix(rnorm(n * p), nrow = n, ncol = p)
y <- x[,1] * 2 + x[,2] * 2.5 + rnorm(n)

## Multi-splitting with lasso.firstq as model selector function
## 'q' must be specified
fit.multi <- multi.split(x, y, model.selector = lasso.firstq,
                        args.model.selector = list(q = 10))

fit.multi
head(fit.multi$pval.corr, 10) ## the first 10 p-values
ci. <- confint(fit.multi)
head(ci.) # the first 6
stopifnot(all.equal(ci.,
                    with(fit.multi, cbind(lci, uci)), check.attributes=FALSE))

## Use default 'lasso.cv' (slower!!) -- incl cluster group testing:
system.time(fit.m2 <- multi.split(x, y, return.selmodels = TRUE))# 9 sec (on "i7")
head(fit.m2$pval.corr) ## the first 6 p-values
head(confint(fit.m2)) ## the first 6 95% conf.intervals

## Now do cluster group testing
```

```

c1GTst <- fit.m2$clusterGroupTest
names(envGT <- environment(c1GTst))# about 14
if(!interactive()) # if you are curious (and advanced):
  print(ls.str(envGT), max = 0)
stopifnot(identical(c1GTst, envGT$clusterGroupTest))
ccc <- c1GTst()
str(ccc)
ccc$hh # the clustering
has.1.or.2 <- sapply(ccc$clusters,
  function(j.set) any(c(1,2) %in% j.set))
ccc$pval[ has.1.or.2] ## all very small
ccc$pval[!has.1.or.2] ## all 1

```

plot.clusterGroupBound

Plot output of hierarchical testing of groups of variables

Description

The `plot()` method for "`clusterGroupBound`" objects plots the outcome of applying a lower bound on the l1-norm on groups of variables in a hierarchical clustering tree.

Usage

```

## S3 method for class 'clusterGroupBound'
plot(x, cexfactor = 1, yaxis = "members",
     xlab = "", col = NULL, pch = 20, ...)

```

Arguments

<code>x</code>	an object of class " <code>clusterGroupBound</code> ", as resulting from <code>clusterGroupBound()</code> .
<code>cexfactor</code>	numeric expansion factor for the size of the node symbols.
<code>yaxis</code>	a string; for the default " <code>members</code> ", the hierarchical tree is shown as function of cluster size on the y-axis, whereas the node sizes are proportional to the lower l1-norm of the respective groups of variables. If <code>yaxis</code> takes any different value, then this is reversed and the tree is shown against the lower l1-norm on the y-axis, while node sizes are now proportional to the number of elements in each cluster.
<code>xlab</code>	label used for the x-axis; by default none.
<code>col</code>	the colour of the symbols for the nodes.
<code>pch</code>	the plot symbol (see points) of the symbols for the nodes.
<code>...</code>	optional additional arguments passed to <code>plot.default</code> .

Value

Nothing is returned

Author(s)

Nicolai Meinshausen <meinshausen@stat.math.ethz.ch>

See Also

Use `clusterGroupBound()` to test all groups in a hierarchical clustering tree. Use `groupBound()` to compute the lower bound for selected groups of variables.

Examples

```
## Create a regression problem with correlated design (n = 10, p = 3):
## a block of size 2 and a block of size 1, within-block correlation is 0.99

set.seed(29)
p <- 3
n <- 10

Sigma <- diag(p)
Sigma[1,2] <- Sigma[2,1] <- 0.99

x <- matrix(rnorm(n * p), nrow = n) %%% chol(Sigma)

## Create response with active variable 1
beta <- rep(0, p)
beta[1] <- 5

y <- as.numeric(x %%% beta + rnorm(n))

## Compute the lower bound for all groups in a hierarchical clustering tree
cgb5 <- clusterGroupBound(x, y, nsplit = 4) ## use larger value for nsplit!

## Plot the tree with y-axis proportional to the (log) of the number of
## group members and node sizes proportional to the lower l1-norm bound.
plot(cgb5)

## Show the lower bound on the y-axis and node sizes proportional to
## number of group members
plot(cgb5, yaxis = "")
```

riboflavin

Riboflavin data set

Description

Dataset of riboflavin production by *Bacillus subtilis* containing $n = 71$ observations of $p = 4088$ predictors (gene expressions) and a one-dimensional response (riboflavin production).

Usage

```
data(riboflavin)
```

Format

y Log-transformed riboflavin production rate (original name: q_RIBFLV).
x (Co-)variables measuring the logarithm of the expression level of 4088 genes.

Details

Data kindly provided by DSM (Switzerland).

References

Bühlmann, P., Kalisch, M. and Meier, L. (2014) *High-dimensional statistics with a view towards applications in biology*. Annual Review of Statistics and its Applications **1**, 255–278

Examples

```
data(riboflavin)
```

```
ridge.proj
```

P-values based on ridge projection method

Description

Compute p-values for lasso-type regression coefficients based on the ridge projection method.

Usage

```
ridge.proj(x, y, family = "gaussian", standardize = TRUE,
           lambda = 1, betainit = "cv lasso", sigma = NULL,
           suppress.grouptest = FALSE,
           multiplecorr.method = "holm", N = 10000)
```

Arguments

x	design matrix (without intercept).
y	response vector.
family	family
standardize	Should design matrix be standardized to unit column standard deviation (logical)?
lambda	Value of penalty parameter lambda (ridge regression).
betainit	Either a numeric vector, corresponding to a sparse estimate of the coefficient vector, or the method to be used for the initial estimation, "scaled lasso" or "cv lasso".

sigma	Estimate of the standard deviation of the error term. This estimate needs to be compatible with the initial estimate (see <code>betainit</code>) provided or calculated. Otherwise, results won't be correct.
<code>suppress.grouptest</code>	A boolean to optionally suppress the preparations made for testing groups. This will avoid quite a bit of computation and memory usage. The output will also be smaller.
<code>multiplecorr.method</code>	Either "WY" or any of <code>p.adjust.methods</code> .
N	number of empirical samples (only used if <code>multiplecorr.method = "WY"</code>).

Value

<code>pval</code>	Individual p-values for each parameter.
<code>pval.corr</code>	Multiple testing corrected p-values for each parameter.
<code>groupTest</code>	Function to perform groupwise tests. Groups are indicated using an index vector with entries in $1, \dots, p$ or a list thereof.
<code>clusterGroupTest</code>	Function to perform groupwise tests based on hierarchical clustering. You can either provide a distance matrix and clustering method or the output of hierarchical clustering from the function <code>hclust</code> as for <code>clusterGroupBound</code> . P-values are adjusted for multiple testing.
<code>sigmahat</code>	$\hat{\sigma}$ coming from the scaled lasso.

Author(s)

Peter Buehlmann, Ruben Dezeure, Lukas Meier

References

Bühlmann, P. (2013) Statistical significance in high-dimensional linear models. *Bernoulli* **19**, 1212–1242.

Examples

```
x <- matrix(rnorm(100 * 100), nrow = 100, ncol = 100)
y <- x[,1] + x[,2] + rnorm(100)
fit.ridge <- ridge.proj(x, y)
which(fit.ridge$pval.corr < 0.05)

## Use the scaled lasso for the initial estimate
fit.ridge.scaled <- ridge.proj(x, y, betainit = "scaled lasso")
which(fit.ridge.scaled$pval.corr < 0.05)

## Group-wise testing of the first two coefficients
fit.ridge$groupTest(1:2)

## Hierarchical testing using distance matrix based on
## correlation matrix
```

```

out.clust <- fit.ridge$clusterGroupTest()
plot(out.clust)

## Fit the method without doing the preparations
## for group testing (saves time and memory)
fit.ridge.faster <- ridge.proj(x, y, suppress.grouptest = TRUE)

```

rXb

Generate Data Design Matrix X and Coefficient Vector β **Description**

Generate a random design matrix X and coefficient vector β useful for simulations of (high dimensional) linear models. In particular, the function `rXb()` can be used to exactly recreate the reference linear model datasets of the hdi paper.

Usage

```

rXb(n, p, s0,
    xtype = c("toeplitz", "exp.decay", "equi.corr"),
    btype = "U[-2,2]",
    permuted = FALSE, iteration = NA, do2S = TRUE,
    x.par = switch(xtype,
                  "toeplitz" = 0.9,
                  "equi.corr" = 0.8,
                  "exp.decay" = c(0.4, 5)),
    verbose = TRUE)

rX(n, p, xtype, permuted, do2S = TRUE,
   par = switch(xtype,
                "toeplitz" = 0.9,
                "equi.corr" = 0.8,
                "exp.decay" = c(0.4, 5)))

```

Arguments

<code>n</code>	integer; the sample size n (paper had always $n = 100$).
<code>p</code>	integer; the number of coefficients in the linear model. (paper had always $p = 500$).
<code>s0</code>	integer number of <i>nonzero</i> coefficients desired in the model; hence at most p .
<code>xtype</code>	a character string specifying the type of design matrix one wants to generate. Must be one of "toeplitz", "equi.corr" or "exp.decay".
<code>btype</code>	a character string specifying the type of nonzero coefficients ("beta") one wants to generate. In the hdi paper, this has been one of "U[-2,2]", "U[0,2]", "U[0,4]", "bfix1", "bfix2" and "bfix10". In general, any string of the form "U[a,b]" or "bfix<c>" is allowed, where a , b , and $\langle c \rangle$ must be numbers (with $a \leq b$).

permuted	logical specifying if the columns of the design matrix should be permuted.
iteration	integer or NA specifying if seeds should be set to generate reproducible realizations of the design type and coefficients type. NA corresponds to not setting seeds. Iteration numbers 1 to 50 correspond to the setups from the paper. If a seed is set, the original <code>.Random.seed</code> at the point of entering the function is saved and is restored upon exit of the data generation. If NA, the current <code>.Random.seed</code> is taken as usual in R.
do2S	logical indicating if in the case of xtypes "toeplitz" or "equi.corr", the $p \times p$ covariance matrix should be inverted twice. Must be true, to regenerate the X matrices from the hdi paper exactly "to the last bit".
x.par, par	the parameters to be used for the design matrix. Must be a numeric vector of length one or two. The default uses the parameters also used in the hdi paper.
verbose	should the function give a message if seeds are being set? (logical).

Details

Generation of the design matrix X :

For all xtype's, the X matrix will be multivariate normal, with mean zero and (co)variance matrix $\Sigma = C$ determined from xtype, x.par and p as follows:

xtype = "toeplitz": $C \leftarrow \text{par} \wedge \text{abs}(\text{toeplitz}(0:(p-1)))$

xtype = "equi.corr": $\Sigma_{i,j} = \text{par}$ for $i \neq j$, and $= 1$ for $i = j$, i.e., on the diagonal.

xtype = "exp.decay": $C \leftarrow \text{solve}(\text{par}[1] \wedge \text{abs}(\text{toeplitz}(0:(p-1))) / \text{par}[2])$

Value

For rXb(): A `list` with components

x the generated $n \times p$ design matrix X .

beta the generated coefficient vector β ('beta').

For rX(): the generated $n \times p$ design matrix X .

Author(s)

Ruben Dezeure <dezeure@stat.math.ethz.ch>

References

Dezeure, R., Bühlmann, P., Meier, L. and Meinshausen, N. (2015) High-dimensional inference: confidence intervals, p-values and R-software hdi. *Statistical Science* **30**, 533–558.

Examples

```
## Generate the first realization of the linear model with design matrix
## type Toeplitz and coefficients type uniform between -2 and 2

dset <- rXb(n = 80, p = 20, s0 = 3,
           xtype = "toeplitz", btype = "U[-2,2]")
x <- dset$x
```

```

beta <- dset$beta

## generate 100 response vectors of this linear model
y <- as.vector( x %*% beta ) + replicate(100, rnorm(nrow(x)))

## Use 'beta_min' fulfilling beta's (non standard 'btype'):
str(ds2 <- rXb(n = 50, p = 12, s0 = 3,
             xtype = "exp.decay", btype = "U[0.1, 5]"))

## Generate a design matrix of type "toeplitz"
set.seed(3) # making it reproducible
X3 <- rX(n = 800, p = 500, xtype = "toeplitz", permuted = FALSE)

## permute the columns
set.seed(3)
Xp <- rX(n = 800, p = 500, xtype = "toeplitz", permuted = TRUE)

```

stability

Function to perform stability selection

Description

Function to perform stability selection

Usage

```

stability(x, y, EV, threshold = 0.75, B = 100, fraction = 0.5,
          model.selector = lasso.firstq, args.model.selector = NULL,
          parallel = FALSE, ncores = getOption("mc.cores", 2L),
          verbose = FALSE)

```

Arguments

x	Design matrix (without intercept).
y	Response vector.
EV	Bound for expected number of false positives.
threshold	Threshold for selection frequency. Must be in (0.5, 1).
B	Number of sub-sample iterations.
fraction	Fraction of data used at each of the B sub-samples.
model.selector	Function to perform model selection. Default is <code>lasso.firstq</code> . User supplied function must have at least three arguments: x (the design matrix), y (the response vector) and q (the maximal model size). Return value is the index vector of selected columns. See <code>lasso.firstq</code> for an example. Additional arguments can be passed through <code>args.model.selector</code> .
args.model.selector	Named list of further arguments for function <code>model.selector</code> .

parallel	Should parallelization be used? (logical)
ncores	Number of cores used for parallelization.
verbose	Should information be printed out while computing (logical).

Value

selected	Vector of selected predictors.
freq	Vector of selection frequencies.
q	Size of fitted models in order to control error rate at desired level.

Author(s)

Lukas Meier

References

Meinshausen, N. and Bühlmann, P. (2010) Stability selection (with discussion). *Journal of the Royal Statistical Society: Series B* **72**, 417–473.

Bühlmann, P., Kalisch, M. and Meier, L. (2014) *High-dimensional statistics with a view towards applications in biology*. *Annual Review of Statistics and its Applications* **1**, 255–278

Examples

```
x <- matrix(rnorm(100 * 1000), nrow = 100, ncol = 1000)
y <- x[,1] * 2 + x[,2] * 2.5 + rnorm(100)
fit.stab <- stability(x, y, EV = 1)
fit.stab
fit.stab$freq[1:10] ## selection frequency of the first 10 predictors
```

Index

- * **confidence intervals**
 - clusterGroupBound, 6
 - groupBound, 11
 - plot.clusterGroupBound, 24
- * **datagen**
 - rXb, 28
- * **datasets**
 - riboflavin, 25
- * **generate datasets**
 - rXb, 28
- * **hierarchical clustering**
 - clusterGroupBound, 6
 - plot.clusterGroupBound, 24
- * **htest**
 - plot.clusterGroupBound, 24
- * **models**
 - boot.lasso.proj, 4
 - fdr.adjust, 9
 - glm.pval, 10
 - hdi, 13
 - lasso.cv, 15
 - lasso.firstq, 16
 - lasso.proj, 17
 - lm.ci, 19
 - lm.pval, 20
 - multi.split, 21
 - ridge.proj, 26
 - stability, 30
- * **package**
 - hdi-package, 2
- * **regression**
 - boot.lasso.proj, 4
 - clusterGroupBound, 6
 - fdr.adjust, 9
 - glm.pval, 10
 - groupBound, 11
 - hdi, 13
 - lasso.cv, 15
 - lasso.firstq, 16
 - lasso.proj, 17
 - lm.ci, 19
 - lm.pval, 20
 - multi.split, 21
 - plot.clusterGroupBound, 24
 - ridge.proj, 26
 - rXb, 28
 - stability, 30
 - .Random.seed, 29
- boot.lasso.proj, 4
- character, 7, 28
- class, 24
- clusterGroupBound, 6, 12, 18, 23–25, 27
- cv.glmnet, 15, 16
- dist, 7
- fdr.adjust, 9
- function, 22
- glm, 10
- glm.pval, 10
- glmnet, 16
- groupBound, 8, 11, 25
- hclust, 7, 18, 23, 27
- hdi, 10, 13, 16, 20, 21
- hdi-package, 2
- lasso.cv, 13, 15, 16, 22, 23
- lasso.firstq, 13, 16, 16, 22, 23, 30
- lasso.proj, 17
- list, 11, 22, 29
- lm, 20
- lm.ci, 19, 22, 23
- lm.pval, 14, 20, 22, 23
- logical, 22
- mclapply, 22

multi.split, [14](#), [21](#)

p.adjust, [9](#)

p.adjust.methods, [4](#), [17](#), [27](#)

plot, [24](#)

plot.clusterGroupBound, [24](#)

plot.default, [24](#)

points, [24](#)

riboflavin, [25](#)

ridge.proj, [26](#)

rX (rXb), [28](#)

rXb, [28](#)

stability, [14](#), [30](#)